

General Disclaimer

One or more of the Following Statements may affect this Document

- This document has been reproduced from the best copy furnished by the organizational source. It is being released in the interest of making available as much information as possible.
- This document may contain data, which exceeds the sheet parameters. It was furnished in this condition by the organizational source and is the best copy available.
- This document may contain tone-on-tone or color graphs, charts and/or pictures, which have been reproduced in black and white.
- This document is paginated as submitted by the original source.
- Portions of this document are not fully legible due to the historical nature of some of the material. However, it is the best reproduction available from the original submission.

NASA CR-167757

TR-82-57

Copy No. 4

**COMPUTER MODELING OF A WIDESWATH SAR CONCEPT
EMPLOYING MULTIPLE ANTENNA BEAM FORMATION TECHNIQUES**

Final Technical Report under Contract NAS9-16437

James M. Estes

**APPLIED RESEARCH LABORATORIES
THE UNIVERSITY OF TEXAS AT AUSTIN
POST OFFICE BOX 8029, AUSTIN, TEXAS 78712-8029**

9 September 1982

Final Report

28 September 1981 - 27 June 1982



Prepared for:

**NATIONAL AERONAUTICS AND SPACE ADMINISTRATION
LYNDON B. JOHNSON SPACE CENTER
HOUSTON, TX 77058**



(NASA-CR-167757) COMPUTER MODELING OF A
WIDESWATH SAR CONCEPT EMPLOYING MULTIPLE
ANTENNA BEAM FORMATION TECHNIQUES Final
Report, 28 Sep. 1981 - 27 Jun. 1982 (Texas
Univ.) 54 p HC A04/MF A01

N83-12305

Unclassified
G3/32 01128

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

| REPORT DOCUMENTATION PAGE | | READ INSTRUCTIONS BEFORE COMPLETING FORM |
|--|-----------------------|---|
| 1. REPORT NUMBER | 2. GOVT ACCESSION NO. | 3. RECIPIENT'S CATALOG NUMBER |
| 4. TITLE (and Subtitle) COMPUTER MODELING OF A WIDESWATH SAR CONCEPT EMPLOYING MULTIPLE ANTENNA BEAM FORMATION TECHNIQUES FINAL REPORT UNDER CONTRACT NAS9-16437 | | 5. TYPE OF REPORT & PERIOD COVERED Final Report 28 Sept 1981 - 27 June 1982 |
| 7. AUTHOR(s) James M. Estes | | 6. PERFORMING ORG. REPORT NUMBER ARL-TR-82-57 |
| 9. PERFORMING ORGANIZATION NAME AND ADDRESS Applied Research Laboratories The University of Texas at Austin Austin, TX 78712-8029 | | 10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS |
| 11. CONTROLLING OFFICE NAME AND ADDRESS National Aeronautics and Space Administration Lyndon B. Johnson Space Center Houston, TX 77058 | | 12. REPORT DATE 9 September 1982 |
| | | 13. NUMBER OF PAGES 50 |
| 14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office) | | 15. SECURITY CLASS. (of this report) UNCLASSIFIED |
| | | 15a. DECLASSIFICATION/DOWNGRADING SCHEDULE |
| 16. DISTRIBUTION STATEMENT (of this Report) | | |
| 17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report) | | |
| 18. SUPPLEMENTARY NOTES | | |
| 19. KEY WORDS (Continue on reverse side if necessary and identify by block number) synthetic aperture radar orbital SAR simulation wideswath SAR | | |
| 20. ABSTRACT (Continue on reverse side if necessary and identify by block number) A technique for wideswath synthetic aperture radar coverage, developed at the Texas A&M's Remote Sensing Center, was implemented into the ARL:UT OSS (orbital sar simulation) computer programs. This report describes the OSS modifications, and the implementation and simulation of the concept. The wideswath technique uses formed multiple antenna beams. | | |

PRECEDING PAGE BLANK NOT FILMED

TABLE OF CONTENTS

| | <u>Page</u> |
|--|-------------|
| LIST OF FIGURES | v |
| I. INTRODUCTION | 1 |
| II. MULTIBEAM CONCEPT | 3 |
| III. IMPLEMENTATION OF A MULTIBEAM COMPUTER SIMULATION | 7 |
| A. Strategy for the Verification of the Multibeam Concept | 7 |
| B. Limitations of the Orbital SAR Simulation's Adaptability to the Multibeam Technique | 8 |
| C. Procedure for Execution of the Multibeam Simulation | 9 |
| IV. COMPUTER PROGRAMS | 11 |
| A. Overview of Program Additions for the OSS | 11 |
| B. Program MECHO | 12 |
| C. Program MBEAM | 13 |
| D. Data Exchange Programs | 14 |
| V. MULTIBEAM SIMULATION RESULTS | 15 |
| A. First Model | 15 |
| B. Second Model | 22 |
| VI. CONCLUSIONS | 27 |
| APPENDIX A - LISTING OF PROGRAM MECHO | 29 |
| APPENDIX B - LISTING OF PROGRAM MBEAM | 41 |

PRECEDING PAGE BLANK NOT FILMED

LIST OF FIGURES

| <u>Figure</u> | | <u>Page</u> |
|---------------|---|-------------|
| 1 | The Geometry of the Multiple Beam SAR | 4 |
| 2 | Multibeam Formation Geometry | 5 |
| 3 | One-Way Antenna Beam Patterns of an Antenna Element | 16 |
| 4 | SARCON Data - Multibeam Model 1 | 18 |
| 5 | Terrain Plot of the Ambiguity Locations for the Multibeam Model | 19 |
| 6 | Terrain Model for the First Multibeam Simulation | 20 |
| 7 | Images from the First Multibeam Simulation | 21 |
| 8 | Terrain Model for the Second Multibeam Simulation | 23 |
| 9 | SARCON Data - Multibeam Model 2 | 24 |
| 10 | Images from the Second Multibeam Simulation | 25 |

I. INTRODUCTION

Under NASA Contracts NAS9-15401 and NAS9-15217, Subtask 1, Applied Research Laboratories, The University of Texas at Austin (ARL:UT), developed a computer simulation of an orbiting synthetic aperture radar (SAR). The simulation is a computer model of a terrain to be imaged, an antenna pattern to be used in the imaging, and the complete specification of a satellite orbit along with radar system parameters (e.g., range pulse compression codes and length, radar orientation with respect to a defined planet, SAR image patch centers and offsets, pulse repetition frequency (PRF), etc). The simulation uses these inputs and "flies" the terrain model placed on a planet (of user specified mass, size, and shape). Synthetic in-phase/quadrature (I/Q) video data are generated, just as in a real system. These data are then processed through a SAR processor and an image of the terrain model is created for analysis. The set of computer programs written and documented¹ under the abovementioned contracts are known collectively as the orbital SAR simulation (OSS). The OSS provides a powerful tool for analysis of proposed orbital SAR concepts as well as parametric SAR studies, etc.

This report under Contract NAS9-16437 describes the effort undertaken by ARL:UT to verify a concept for an orbital SAR. The concept was developed at the Remote Sensing Center, Texas A&M University (TAMU/RSC), and makes use of simultaneously formed antenna beams along the surface of a cone intersected by the ground plane. The technique, known as multibeam formation, has been documented.² The OSS was adapted to incorporate the basic ideas of this technique; then the model was executed to verify the feasibility of the concept.

PRECEDING PAGE BLANK NOT FILMED

II. MULTIBEAM CONCEPT

The multibeam technique allows wide swath SAR image coverage at a constant angle of incidence (but not aspect). By properly combining the phased and weighted outputs of multiple receiving antenna elements in an array antenna, multiple simultaneous beams may be created; see Fig. 1.³ These beams are formed along a cone of half-angle θ_0 . One of the antenna array elements acts as a transmitter which transmits a real beam of angle ψ in the image plane and has a narrow beamwidth in the elevation plane β_e . In addition to the wide swath coverage, the narrow elevation beamwidth permits the use of a high PRF (due to the short unambiguous slant range interval), thus reducing transmitter peak power and providing reduced ambiguity levels in the Doppler dimension because of the increased Doppler sampling rate, i.e., the PRF.

The multiple beams are created by combining the outputs of the receiving antennas with proper phase shifts applied to each element. Referring to Fig. 2,⁴ the phase shift α_i between each element required to point the i th beam in the θ_i direction is

$$\alpha_i = \frac{2\pi d_h \sin\theta_0 \sin(\phi_i - \phi_0)}{\lambda} ,$$

where d_h is the spacing between the antenna elements and λ is the transmitted wavelength.⁵ Thus the basic operation required to generate the i th beam is to implement the following sum over the N antenna receiving elements

ORIGINAL PAGE IS
OF POOR QUALITY

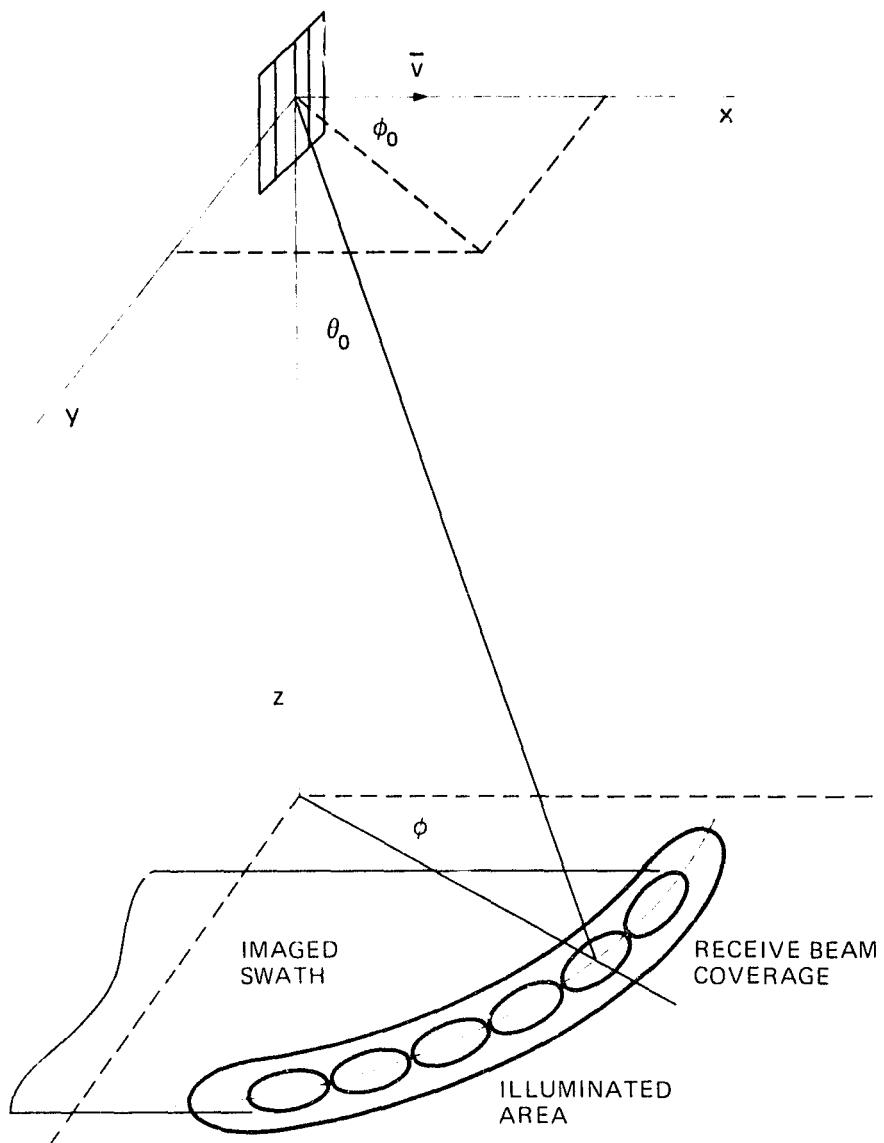


FIGURE 1
THE GEOMETRY OF THE MULTIPLE BEAM SAR

ARL UT
AE-81-137
CRG - GA
9 - 16 - 81

ORIGINAL MULTIBEAM
OF POOR QUALITY

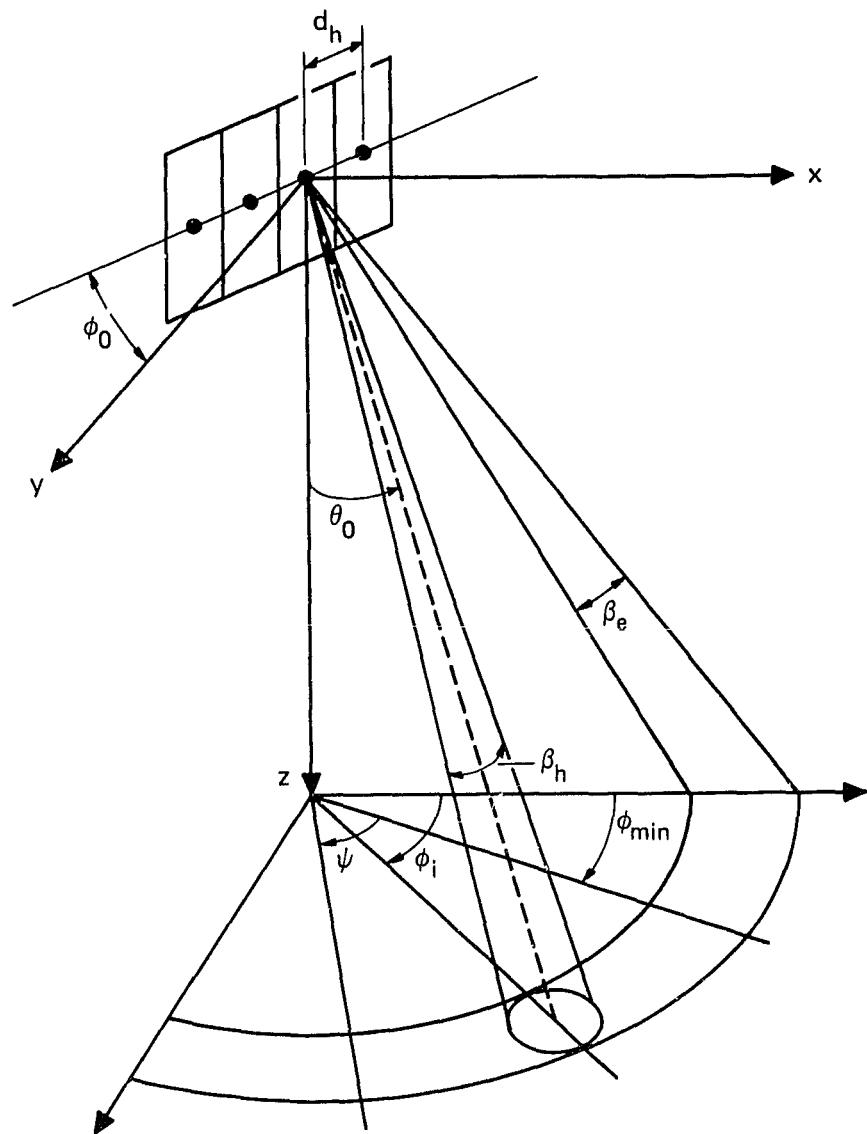


FIGURE 2
MULTIBEAM FORMATION GEOMETRY

ARL:UT
AS-82-1481
JME - GA
9-10-82

$$E_i = \sum_{n=0}^{N-1} E_n e^{-j n \alpha_i}$$

where E_n is the sampled output of the signal of the n th receiving element.⁶ Finally, the first-null beamwidth of the formed beam is⁷

$$\beta_h \text{ (1st null)} = \arcsin \left[\sin(\phi_i - \phi_0) + \frac{\lambda}{Nd_h \sin \theta_0} \right] - \arcsin \left[\sin(\phi_i - \phi_0) - \frac{\lambda}{Nd_h \sin \theta_0} \right]$$

ORIGINAL PAGE IS
OF POOR QUALITY

III. IMPLEMENTATION OF A MULTIBEAM COMPUTER SIMULATION

A. Strategy for the Verification of the Multibeam Concept

Due to limitations in the flexibility of the OSS and limited time and computer resources, a full simulation of the multibeam concept utilizing the outputs of all the formed beams for full wideswath coverage was impractical. The approach taken was to create a squint mode model with specified parameters (such as the antenna 3 dB beamwidth) which correspond to those of one beam formed from a multibeam model. In this way the maximum compatibility with the current OSS configuration was achieved.

The OSS calculates the PRF and some of the other parameters based on the specifications of one of the multibeams to be formed. When the simulation is executed, the phase centers of the antenna elements making up the antenna array for multibeam processing are specified. Synthetic I/Q video is created from each receiving element; one of the elements is also used to transmit a real beam antenna pattern with the beamwidth necessary to encompass all the possible formed beams. Since the OSS-multibeam model is specified with an antenna beamwidth less than that used when the I/Q data are formed, processing of the I/Q data from any one of the elements (without multibeam formation) should produce an image containing ambiguities; these ambiguities can be suppressed by processing the I/Q data resulting from the multibeam formation between all the antenna elements. It is possible to process the I/Q data from one antenna element and from one of the formed beams to demonstrate the amount of ambiguity suppression.

To minimize the amount of computer time necessary to execute the multibeam simulation, an OSS feature is used to locate the points in a

terrain model (given the planet, orbit, radar, and synthetic array formation specifications) which will map ambiguously into the patch center of the created image if not suppressed by the proper antenna pattern.⁸ Placing scatterers around these points makes full use of the point scatterers' terrain positions and minimizes the number of scatterers needed in a terrain model to demonstrate suppression by the multibeam technique. The computer time required to execute a simulation is proportional to the number of scatterers in the terrain model.

While the approach taken does not fully test the multibeam concept as it would be implemented in a real system, it does demonstrate some of the advantages and disadvantages associated with the radar, orbit, and antenna pattern specifications for multibeam formation. Aside from the use of a single beam instead of all the possible beams, the greatest departure of the multibeam simulation from a real implementation is in the signal processing and image formation process. The OSS processes the I/Q data into an imaged patch perpendicular to the line of sight (LOS) of the antenna boresight (or formed beam), thus not taking full advantage of the simplicities of the multibeam geometry; however, this does not detract from the verification of the multibeam formation technique.

B. Limitations of the Orbital SAR Simulation's Adaptability to the Multibeam Technique

The current implementation of the OSS terrain modeling and image formation procedures place some severe restrictions on possible multibeam implementations. An OSS terrain model is created by specifying two-dimensional coordinate positions at which point scatterers are specified along with a relative scattering intensity. The coordinate system is defined such that $(0,0)$ is the center of the terrain model and it will be the patch center of the imaged area. This presents no problem for creating I/Q data for the multibeam simulation; however, it makes it difficult to process images from beams not formed about the patch center. For this reason, we concentrated on forming

and imaging only one arbitrary beam, whose coordinates are chosen prior to the start of OSS execution. Simultaneous imaging of more than one beam would require major changes to the signal processing routines and would add little to the demonstration of the multibeam technique, i.e., the problem of beam formation and imaging of each beam is separated from the task of combining all the beam's images into one wide swath image.

Program ECHO is the OSS routine which computes the slant ranges and echo strength levels from the point scatterers. The distance to each scatterer at each orbit position at which a pulse is transmitted must be determined along with the angle to the scatterer from the antenna boresight. Input to ECHO consists of the terrain model, antenna model, and SARCON data created by the controller program, SARTREK. ECHO places the terrain model on the planet; currently this is done by placing the terrain origin center ($0,0$) at a user selected planet latitude and computing the longitude at which the antenna boresight will intersect the selected latitude.⁹ The terrain plane is rotated so that its x axis is perpendicular to the LOS from the radar at some user specified squint and nadir angles. The plane is then radially projected onto the planet's surface. As the radar "flies" the array the distance to the patch center at each transmitted pulse is recorded and the received echo is automatically range gated such that the center sample of the echo always contains the patch center, thus eliminating the need for range walk corrections. The slant range data are used later in the focus operation. To process more than one beam per multibeam simulation run would thus require revision of this procedure and changes to the focus routines. It should be pointed out that all the multiple beams from one model could be generated by repeated runs with changing patch center locations. Again, these restrictions do not detract from the demonstration of the multibeam technique.

C. Procedure for Execution of the Multibeam Simulation

The procedure for execution of a multibeam simulation is similar to that used for execution of the general OSS. OSS programs TERRAIN,

ANTENA, and SARTREK are run to set up the terrain and antenna models, and to specify the general theoretical parameters for a simulation. A program developed for the multibeam simulation, MECHO, replaces the OSS program ECHO. The output file of slant range/echo strength data generated by MECHO is then reorganized into several files, each one identical to the output file that program ECHO creates. There is one echo strength data file for each antenna element in the multibeam antenna array. These files are then processed one at a time into files of synthetic video I/Q samples by OSS program SAMPLE. If range pulse compression processing is selected, then OSS program COMPRES is executed next on each of the I/Q video data files. Program MBEAM, the beam-forming processor, is executed next; MBEAM combines the I/Q data files to form a multibeam at some specified squint angle. Program MBEAM creates a file of I/Q data which is identical in format to the files produced by OSS program SAMPLE. The I/Q video data file for the formed beam is then processed through the remainder of the OSS programs: FOCUS, FILTER, and POST. The output of program POST is sent to the ARL/Hi high resolution image display system for analysis and, optionally, to be photographed.

IV. COMPUTER PROGRAMS

A. Overview of Program Additions for the OSS

The OSS program ECHO has been modified (into program MECHO) to calculate and output the slant range/echo strength data for all the antenna elements in the real antenna array. The multibeam simulation could have been constructed by using one set of SARCON data (output from the controller program SARTREK) and running program ECHO one time for each antenna element specifying the proper phase center for that element (i.e., specifying the position of the element in the real antenna array in orbiter coordinates). However, for a modest size terrain model, ECHO is the most expensive program in the simulation (in terms of computer time), and executing it separately for each antenna element would be very costly. Program MECHO makes use of the redundant coordinate transformations which comprise the greatest expense in the execution of program ECHO.

The output file of MECHO is reorganized into files which are processed by the program SAMPLE (and COMPRES if required) into I/Q video data. Program MBEAM was written to perform the multibeam formation. MBEAM uses the squint and nadir angles stored in the SARCON data recorded on the I/Q video data files. The squint and nadir angles are in the direction of image formation used by the OSS, so MBEAM forms the multibeam in the direction specified by these angles.

Routines were also developed to convert the I/Q floating point data files to files of I/Q data which contain scaled integer values of arbitrary bit precision. A program is available to transfer 32-bit I/Q integer data to computer compatible tape for transfer to other computers. These routines were used to transport data to TAMU/RSC for beam formation and image processing.

B. Program MECHO

A listing of program MECHO is available in Appendix A. It is identical to the OSS program ECHO with the following additions. A file, ANTPOS, has been added for additional input to define the phase center positions of the antenna elements. The positions are defined in the body axis coordinate system of the orbiter.¹⁰ The file is a standard text file and has the structure listed below.

| <u>Line No.</u> | <u>Description</u> |
|-----------------|--|
| 1 | Number of elements in the antenna |
| 2 | X position of element 1, Y position of element 1, Z position of element 1 |
| 3 | X position of element 2, Y position of element 2, Z position of element 2 |
| N+1 | X position of element N, Y position of element N, Z position of element N |

In program ECHO the variables PHCPBX, PHCPBY, and PHCPBZ contain the x, y, and z phase center coordinates, and variables X, Y, and Z contain the phase center coordinates transformed into the Greenwich TOD (true-of-date) coordinate system. In program MECHO, these variables have been made into arrays which contain the element coordinates. These arrays are currently dimensioned at 16 so that an antenna with up to 16 elements may be specified.

In the ECHO programs, all the scatterers are placed on the planet and then transformed into the Greenwich TOD system. After the positions of the orbiter at the pulse transmission locations are computed and transformed into the Greenwich TOD system, the orbiter-to-scatterer distances and echo strength levels are computed. In MECHO, the array

SREL, which stores the computed slant ranges and echo levels, was dimensioned to accommodate all the element positions, whereas this dimension in ECHO was for a single element.

MECHO outputs data sequentially first by pulse, then by element, so that all the data for each element at one pulse position is output, and then all the data for each element at the next pulse position is output, etc. The output file must then be reorganized by the antenna element so that each element's echo data can be input to the next routine, OSS program SAMPLE. This is accomplished by program MEREOORG, which reorders the MECHO output file into ECHO-compatible data files, one file for each element.

C. Program MBEAM

A listing of program MBEAM is included in Appendix B. Program MBEAM uses as input the video I/Q data files generated for the elements of the array antenna along with some interactive input and then produces an I/Q data file for one of the possible multibeams. The interactive input required is specification of the squint angle of the array antenna ϕ_0 and the inter-element spacing of the antenna in meters.

The program reads the SARCON data record from the first I/Q data file, then the SARCON records on the rest of the I/Q data files are skipped positioning the files at the start of the first video data records. The SARCON record is copied to the I/Q data output file. Using the squint angle, nadir angle, and radar wavelength specified in the SARCON data along with entered antenna array squint and element spacing, MBEAM calculates the phase shift to be applied to the video I/Q data from each element of the antenna array according to the equation given in Section II. One record is read from each I/Q data input file; the phase shift for each I/Q data record is applied to every I/Q data point in the record. Next, the corresponding I/Q data points from each record are summed and the resulting data record, the I/Q data of a formed multibeam, is written to the video I/Q data output file. This process is repeated for each set of I/Q data input records.

D. Data Exchange Programs

Programs were written to allow interchange of video I/Q data with TAMU/RSC. ARL:UT and TAMU/RSC jointly agreed on a format for exchange. Since the ARL:UT computer, a Control Data Corporation CYBER, and the TAMU/RSC computer, a Digital Equipment Corporation VAX, do not have the same internal number representation, it was decided that exchange of integer data would be the easiest approach. The programs first calculate statistics on the I/Q data generated by OSS program SAMPLE; these statistics are used to appropriately scale the I/Q data, and then they are converted to 32-bit integer format.

After conversion from the one's complement format (used by the CYBER) to the two's complement format (used by the VAX) the I/Q data are output. One record is output for each received pulse. Each record contains the I/Q data from all the antenna elements, the data for element 1 followed by element 2, etc. Each element's data consist of 256 I/Q samples; if less than 256 samples per element per pulse were synthesized, then each element's data are padded with zeroes to make up the 256 samples.

V. MULTIBEAM SIMULATION RESULTS

A. First Model

The model parameters were jointly specified by ARL:UT and TAMU/RSC with TAMU/RSC supplying the antenna pattern used for the transmitting and receiving elements and the multibeam locations in the ground plane. The rest of the model's parameters closely correspond to the SEASAT-A based parameters used in the test model documented in Ref. 1; thus the non-multibeam simulation's results described are of some use in interpreting the results of the multibeam simulation.

Figure 3 contains the antenna beam patterns used by the transmitting element and the receiving elements of the antenna array. The multibeam parameters are (referring to Figs. 1 and 2)

$$d_h = 1 \text{ m} ,$$

$$\phi_0 = 30^\circ$$

$$\phi \text{ of beams} = 18^\circ, 26^\circ, 34^\circ, 42^\circ ,$$

$$\theta_0 = 20^\circ ,$$

$$SW \approx 150 \text{ km} .$$

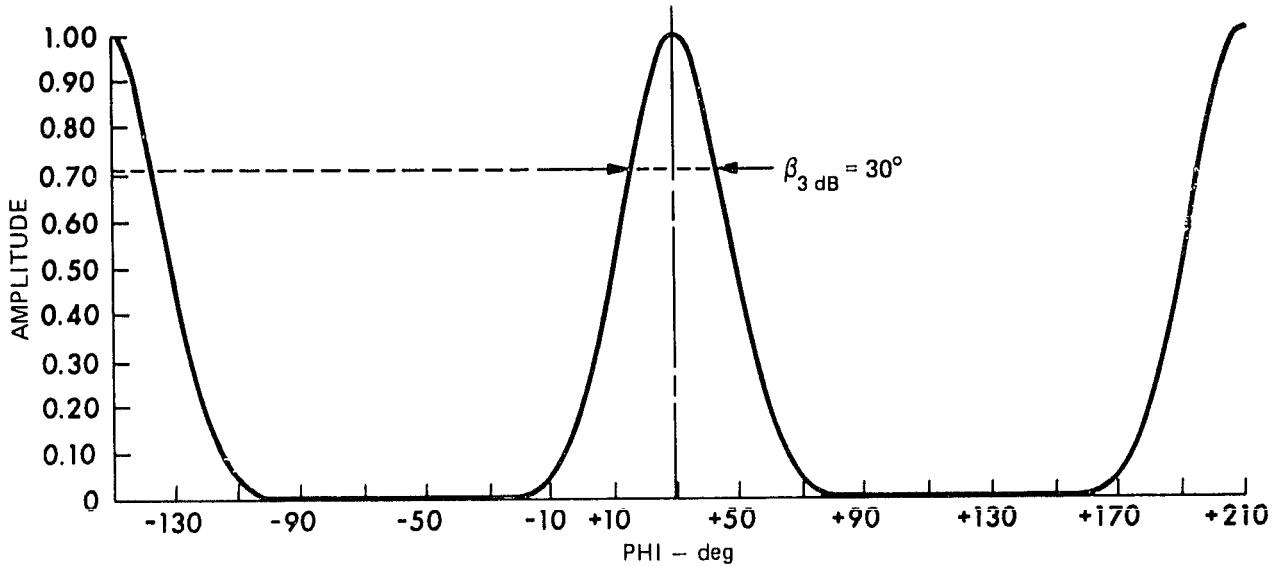
The antenna array contained four elements with phase center positions:

$$(\emptyset, \emptyset, \emptyset) ,$$

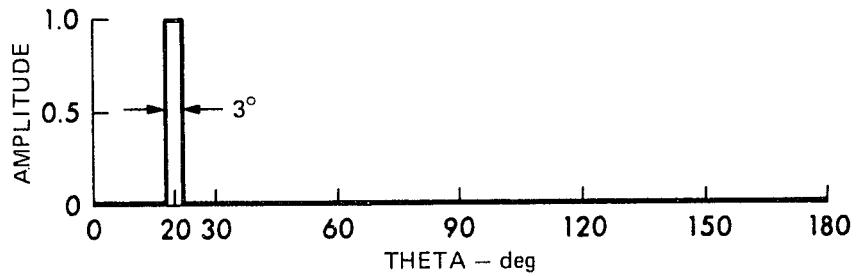
$$(-0.5, 0.866, \emptyset) ,$$

$$(-1, 1.732, \emptyset) ,$$

ORIGINAL PAGE IS
OF POOR QUALITY



(a) AZIMUTH PATTERN



(b) ELEVATION PATTERN

FIGURE 3
ONE-WAY ANTENNA BEAM PATTERNS
OF AN ANTENNA ELEMENT

ARL:UT
AS-82-1482
JME - GA
9-10-82

and

$$(-1.5, 2.598, \theta) .$$

The beamwidth in the x-y plane of a formed beam is 8° . For the simulation execution described herein, only the beam at $\theta=34^{\circ}$ was created and processed.

Figure 4 is a listing of the SARCON data which contains the OSS parameters for the first model. Figure 5 is an OSS produced plot of the ambiguity locations which map into the patch center based on the SARCON data of Fig. 4; imposed on the plot is the radar platform's ground projected location, the platform's velocity vector, and the 3 dB beamwidth of the array antenna's elements (30°). The points which approximately define a circle are azimuth ambiguities (i.e., points at the same slant range as the patch center whose Doppler frequencies will alias into the Doppler frequency of the patch center) while the points lying approximately on a line are range ambiguities (i.e., points which differ in slant range to the radar platform by an amount equal to the distance light travels between two successive radar pulses). Figure 6 contains plots of the scatterer positions for the terrain model used in the first simulation model. The fields were placed at azimuth ambiguity locations so that they would be imaged about the patch center if not suppressed by the beam pattern of the multibeam to be formed. The OSS calculated the SARCON data assuming that a beam pattern of 8° beamwidth was to be used in imaging; however, the 30° real beam pattern was used so that ambiguities will be introduced if the multibeam formation is not performed.

The multibeam simulation was then executed to the point of obtaining I/Q data for each element. The I/Q data from element 1 was processed into an image; since no multibeam processing was performed, we expect to see ambiguities in the image. The I/Q data from all the elements were also processed through the beam formation processor. The results of these simulations are shown in Fig. 7. The suppression of the imaged ambiguities is contrasted in Figs. 7(a) and 7(c);

ORIGINAL PAGE IS
OF POOR QUALITY

| | | |
|---------------------------------------|---|-------------------|
| PLANET NAME ** | PLANET SPECIFICATION | .63781670000E+04 |
| EARTH | EQUATORIAL RADIUS (KM) ** | |
| ECCENTRICITY ** | GRAVITATIONAL CONSTANT (KM3/SEC2) ** | .39860100000E+06 |
| ROTATIONAL RATE (DEG/S) ** | TIME OF PRIME MERIDIAN PASSAGE (S) ** | 0. |
| | | |
| ORBIT I.D. ** | ORBIT SPECIFICATION | .71865400000E+04 |
| ECCENTRICITY ** | SEMI-MAJOR AXIS (KM) ** | |
| LONG OF ASCENDING NODE (DEG) ** | INCLINATION (DEG) ** | .10800000000E+03 |
| TIME OF PERIGEE PASSAGE (S) ** | ARGUMENT OF PERIGEE (DEG) ** | 0. |
| ORBITER INITIALIZATION TIME(S) ** | ROTATIONAL RATE (DEG/S) ** | .59376152657E-01 |
| | | |
| RADAR I.D. ** | RADAR SPECIFICATION | .23500000000E+00 |
| RECIEVER/TRANSMITTER BW (MHZ) ** | SEASAT-A OPERATING WAVELENGTH (M) ** | |
| SIGNAL-TO-NOISE RATIO (DR) ** | RANGE TIME-BANDWIDTH PRODUCT ** | .10000000000E+01 |
| SAMPLE LENGTH OF RANGE CORRELATION ** | A/D SAMPLE RATE (MHZ) ** | .15594580269E+02 |
| BINARY PHASE CODE ** | 1 SAMPLE LENGTH ACROSS PHASE INTERVAL * | 1 |
| GROUND RANGE RESOLUTION (M) ** | R BINARY PHASE CODE SEQUENCE ** | RANDOM |
| RANGE SAMPLING RATIO (M) ** | AZIMUTH RESOLUTION (M) ** | .50000000000E+02 |
| RANGE IMPULSE RESPONSE FUNCTION ** | AZIMUTH SAMPLING RATIO (M) ** | .20000000000E+01 |
| PATCH-TO-PATCH OFFSET, RNG (M) ** | COSINE**? | TAYLOR |
| RANGE SWATH WIDTH (KM) ** | APERTURE WEIGHT FUNCTION ** | |
| MAP START LATITUDE (DEG) ** | PATCH-TO-PATCH OFFSET, AZ (M) ** | 0. |
| | NO OF PATCHES ** | 1 |
| | | |
| ANTENNA I.D. ** | ANTENNA SPECIFICATION | .20000000000E+02 |
| BORE SIGHT SQUINT AT TO (DEG) ** | MULTI-BEAM BORESIGHT NADIR AT TO (DEG) ** | |
| ELEVATION ANGULAR COVERAGE (DEG) ** | AZIMUTH ANGULAR COVERAGE (DEG) ** | .80000000000E+01 |
| PHASE CENTER, BODY AXIS X (M) ** | PHASE CENTER, BODY AXIS X (M) ** | 0. |
| COORD SYS, BODY AXIS ROLL, (DEG) ** | PHASE CENTER, BODY AXIS Z (M) ** | 0. |
| COORD SYS, BODY AXIS PITCH, (DEG) ** | COORD SYS, BODY AXIS PITCH, (DEG) ** | -.70000000000E+02 |
| PLAT PITCH RATE (DEG/S) ** | PLAT ROLL RATE (DEG/S) ** | 0. |
| | PLAT YAW RATE (DEG/S) ** | 0. |
| | | |
| | TERRAIN SPECIFICATION | .52 |
| TERAIN I.D. ** | MULTI-TST1 NO OF DISCRETES ** | 126 |
| NO OF FIELDS ** | 2 TOTAL NO OF SCATTERERS ** | |
| X-AXIS COVERAGE (KM) ** | .26605000000E+03 Y-AXIS COVERAGE (KM) ** | .54950000000E+02 |
| TERRAIN CENTER, R (KM) ** | .63675192370E+04 TERRAIN CENTER, LAT (DEG) ** | .45000000000E+02 |
| TERRAIN CENTER, LONG (DEG) ** | .3402095A470E+03 | |
| | | |
| SYNTHETIC ARRAY NC ** | SYNTHETIC ARRAY PARAMETERS | .75706892121E+03 |
| ARRAY LENGTH (M) ** | 1 TRANSMISSION START TIME (S) ** | |
| ARRAY FORMATION TIME (MS) ** | ARRAY INCLINATION (DEG) ** | .81088631361E-01 |
| NO OF PULSES ** | PLATFORM VELOCITY (KM/S) ** | .74580106359E+01 |
| NO OF RANGE SAMPLES ** | 1758 PRF (HZ) ** | .54629996R35E+04 |
| PATCH CENTER, RANGE SAMPLE NC. ** | 255 NO. OF AZIMUTH FILTERS ** | 255 |
| SLANT RANGE RESOLUTION (M) ** | 128 SLANT RANGE SWATH WIDTH (KM) ** | .24510624417E+01 |
| START RANGE (KM) ** | .19224146775E+02 SLANT RANGE SAMPLE INTERVAL (M) ** | .96120733877E+01 |
| SQ INT ANGL PATCH CENTER (DEG) ** | .86659032998E+03 RANGE PATCH CENTER (KM) ** | .86781106330E+03 |
| LOS AZIMUTH AT PATCH CENTER (DEG) ** | .3412516A752E+02 NADIR ANGLE PATCH CENTFR (DEG) ** | .19946775461E+02 |
| PATCH CENTER, R (KM) ** | -.1701758E+118E+03 LOS INCIDENCE AT PATCH CENTER (DFG) ** | .22611644021E+02 |
| PATCH CENTER, LAT (DEG) ** | .63675192370E+04 ORBITER MASS CENTER, R (KM) ** | .71763842359E+04 |
| PATCH CENTER, LONG (DEG) ** | .45000000000E+02 ORBITER MASS CENTER, LAT (DEG) ** | .42372508999E+02 |
| | ORBITER MASS CENTER, LONG (DEG) ** | .33959432948E+03 |

FIGURE 4
SARCON DATA - MULTIBEAM MODEL 1

ORIGINAL PAGE IS
OF POOR QUALITY

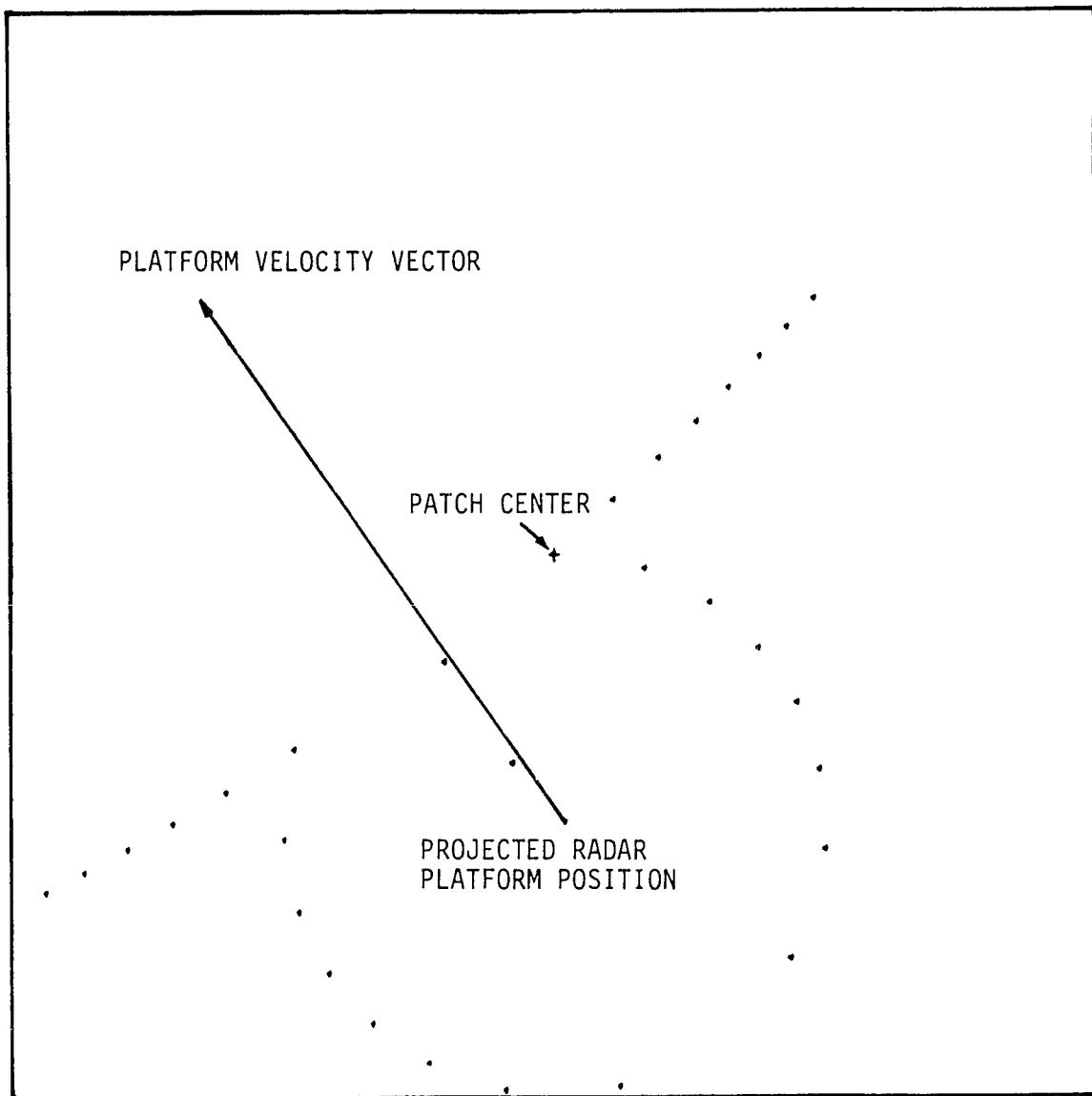
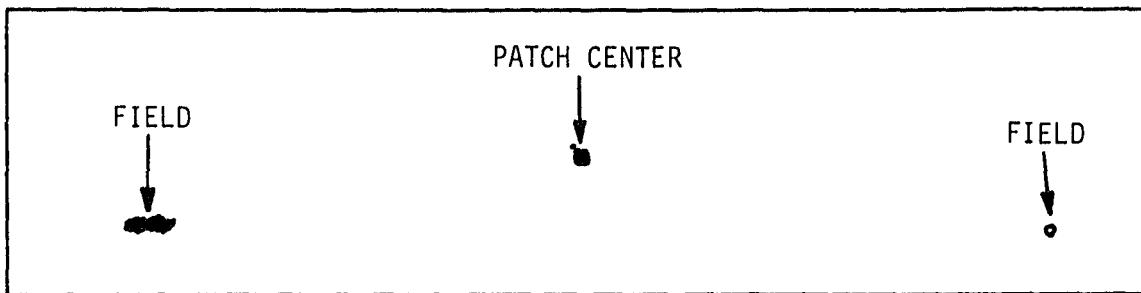
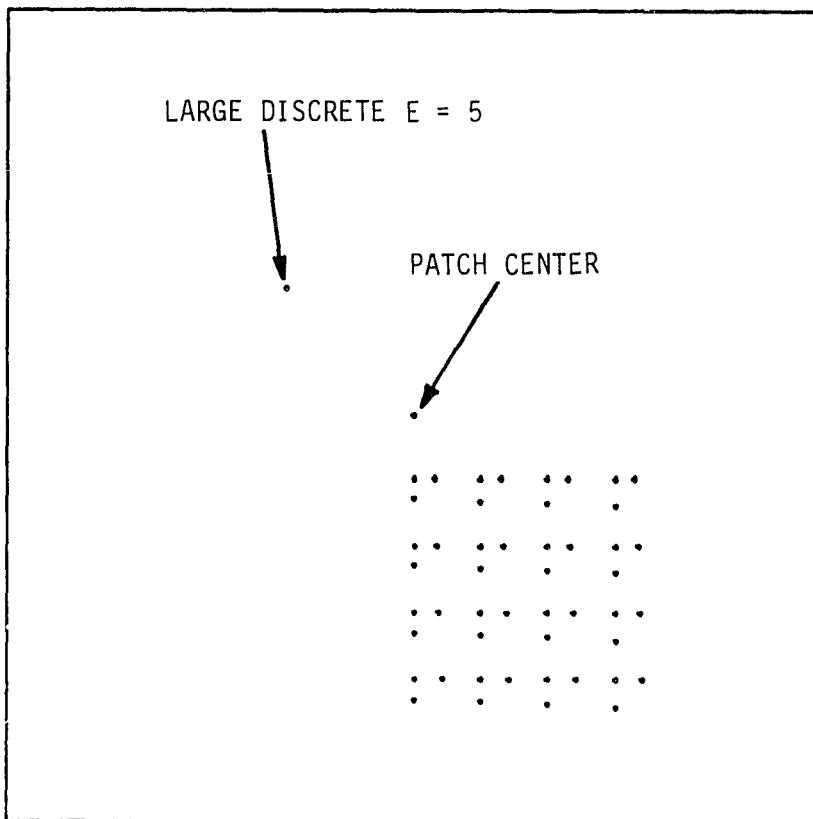


FIGURE 5
TERRAIN PLOT OF THE AMBIGUITY LOCATIONS FOR THE MULTIBEAM MODEL

ORIGINAL PAGE IS
OF POOR QUALITY



(a) COMPLETE TERRAIN MODEL (240 km x 60 km)
Field at right: E=2 All other scatterers: E=1

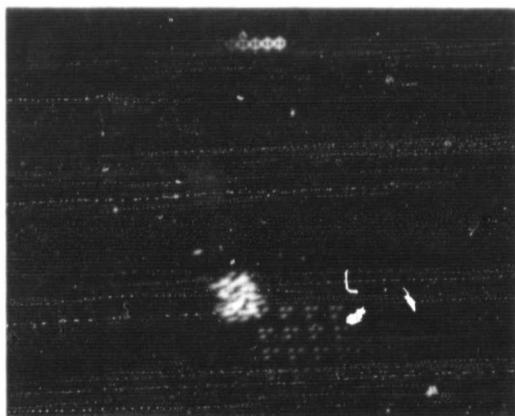


(b) AREA OF THE TERRAIN MODEL TO BE IMAGED
(6.375 km x 6.375 km)

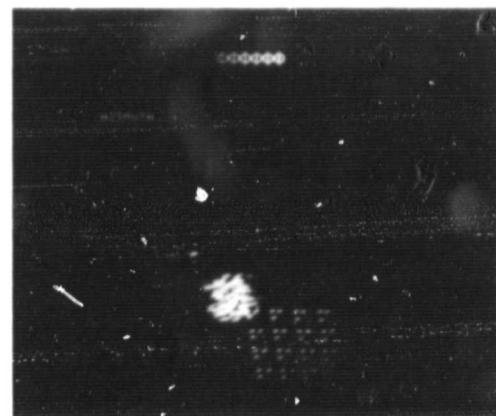
FIGURE 6
TERRAIN MODEL FOR THE FIRST MULTIBEAM SIMULATION
20

AS-82-1486

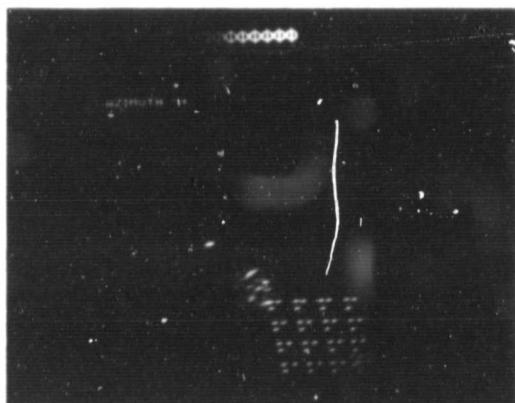
ORIGINAL PAGE IS
OF POOR QUALITY



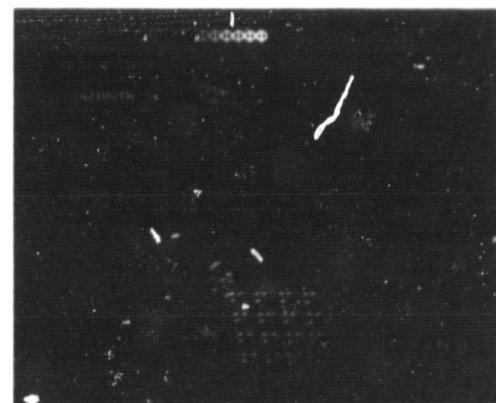
(a)
NO MULTIBEAM PROCESSING
2 dB/GRAY SCALE - 16 SCALES



(b)
NO MULTIBEAM PROCESSING
2 dB/GRAY SCALE - TOP 6 SCALES



(c)
MULTIBEAM PROCESSING
2 dB/GRAY SCALE - 16 SCALES



(d)
MULTIBEAM PROCESSING
2 dB/GRAY SCALE - TOP 6 SCALES

FIGURE 7
IMAGES FROM THE FIRST MULTIBEAM SIMULATION

Figs. 7(b) and 7(d) show only the top 12 dB of the images and demonstrate more clearly the significance of multibeam processing. The beam formation processing was not shaded, and so sidelobes of approximately 13 dB are expected (application of a weighting or shading function to the antenna element outputs should reduce this level); as illustrated in Fig. 7 the level of the imaged ambiguities from the multibeam processing are approximately 13 dB below the level of the imaged ambiguities with no multibeam processing.

The images are observed to be slightly "skewed" in azimuth, a result of the squint mode geometry and OSS image processing. If a line is drawn through the range ambiguity points of Fig. 5 (including the patch center), then all the points on this line have the same Doppler frequency as the patch center. The OSS currently processes all the range bins of one patch (synthetic array) with the same focus and filtering functions and lines up all the azimuth filters into vertical lines. Therefore, the azimuth filters are shifted in the range bins about the range bin containing the patch center. Program POST removed some of the skewing by shifting the azimuth lines based on their position relative to the center range bin.

B. Second Model

Except for the terrain model, the second simulation's parameters are identical to the first simulation discussed above. The section of the terrain model to be imaged is shown in Fig. 8. Fields were placed at the locations shown in Fig. 6, but they consisted of many more scatterers; a total of 933 scatterers were used in the second terrain model compared to only 126 for the first model. Figure 9 contains the SARCON data generated for this simulation.

The resultant images of the simulation are shown in Fig. 10. The photographs show that the multibeam processing suppresses the imaged ambiguity fields by over 12 dB; the fields would probably be less pronounced if the area being imaged contained a background reflectance

ORIGINAL PAGE IS
OF POOR QUALITY

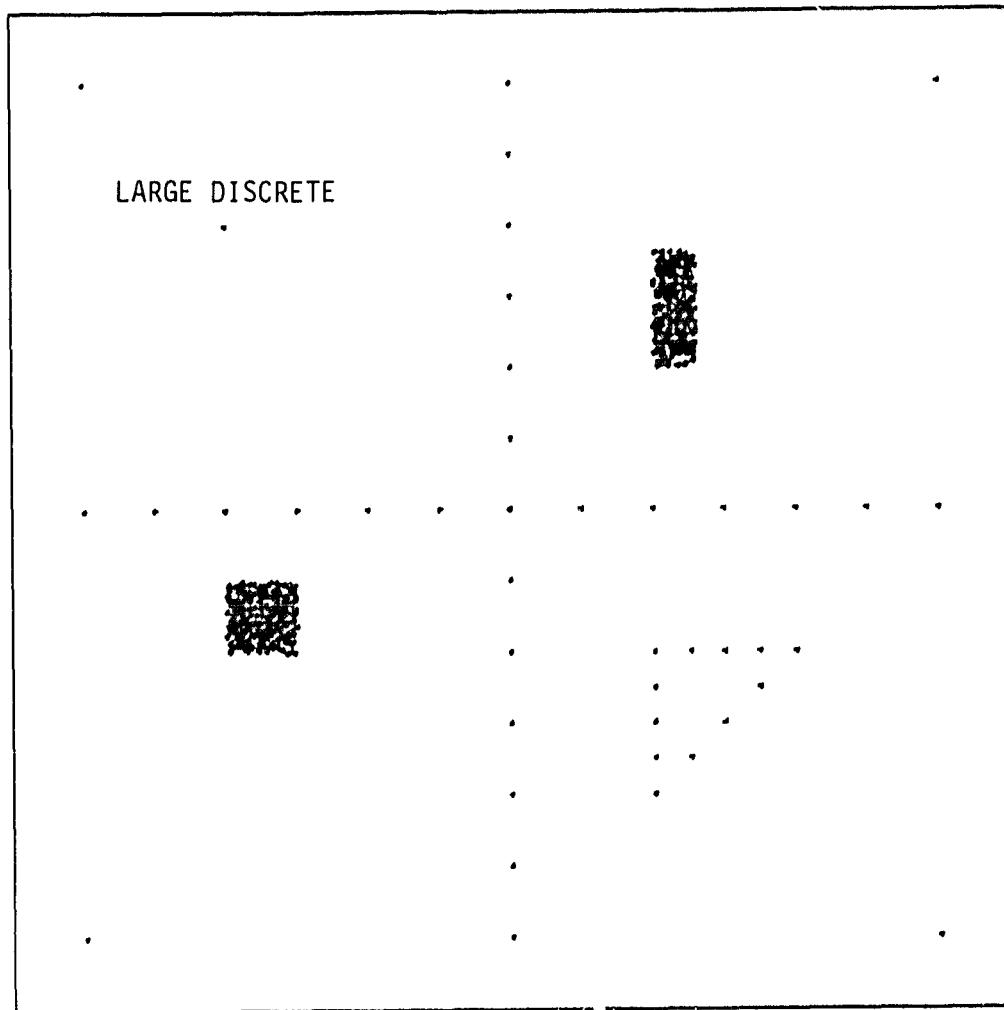


FIGURE 8
TERRAIN MODEL FOR THE SECOND MULTIBEAM SIMULATION

AREA OF THE TERRAIN MODEL TO BE IMAGED
(6.375 km x 6.375 km)

Large Discrete: $E=20$
Field at lower left: $E=0.2$ Field at upper right: $E=0.5$
All other scatterers, including the ambiguity scatterers
not shown on the plot: $E=1$

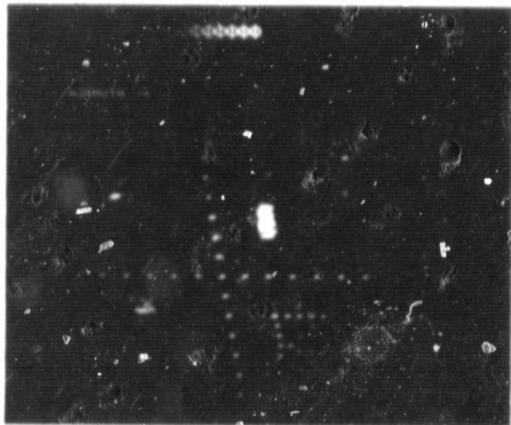
ORIGINAL PAGE IS
OF POOR QUALITY

| | | | | |
|---------------------------------------|----------------------------|------------------------------------|---|-------------------|
| PLANET NAME ** | PLANET SPECIFICATION | EARTH | EOQUATORIAL RADIUS (KM) ** | .63781670000E+04 |
| ECCENTRICITY ** | | | GRAVITATIONAL CONSTANT (KM3/SEC2) ** | .39860100000E+06 |
| ROTATIONAL RATE (DEG/S) ** | | | TIME OF PRIME MERIDIAN PASSAGE (S) ** | 0. |
| ORBIT I.D. ** | ORBIT SPECIFICATION | 794CIRCULR | SEMI-MAJOR AXIS (KM) ** | .71865400000E+04 |
| ECCENTRICITY ** | | .20000000000E-02 | INCLINATION (DEG) ** | .10800000000E+03 |
| LONG OF ASCENDING NODE (DEG) ** | | 0. | ARGUMENT OF PERIGEE (DEG) ** | 0. |
| TIME OF PERIGEE PASSAGE (S) ** | | 0. | ROTATIONAL RATE (DEG/S) ** | .59376152657E-01 |
| ORBITER INITIALIZATION TIME (S) ** | | -.10000000000E-03 | | |
| RADAR I.D. ** | RADAR SPECIFICATION | SEASAT-A | OPERATING WAVELENGTH (M) ** | .23500000000E+00 |
| RECIEVER/TRANSMITTER BW (MHZ) ** | | .779/2901747E+01 | RANGE TIME-FBANDWIDTH PRODUCT ** | .10000000000E+01 |
| SIGNAL-TO-NOISE RATIO (DR) ** | | .10000000000E+03 | A/D SAMPLE RATE (MHZ) ** | .15594580269E+02 |
| SAMPLE LENGTH OF RANGE CORRELATION ** | | | 1 SAMPLE LENGTH ACROSS PHASE INTERVAL * | 1 |
| BINARY PHASE CODE ** | | R | RINARY PHASE CODE SEQUENCE ** | RANDOM |
| GROUND RANGE RESOLUTION (M) ** | | .50000000000E+02 | AZIMUTH RESOLUTION (M) ** | .50000000000E+02 |
| RANGE SAMPLING RATIO (M) ** | | .20000000000E+01 | AZIMUTH SAMPLING RATIO (M) ** | .20000000000E+01 |
| RANGE IMPULSE RESPONSE FUNCTION ** | | COSINE**? | APERTURE WEIGHT FUNCTION ** | TAYLOR |
| PATCH-TU-PATCH OFFSET, RNG (M) ** | | 0. | PATCH-TU-PATCH OFFSET, AZ (M) ** | 0. |
| RANGE SWATH WIDTH (KM) ** | | .63750000000E+01 | NO OF PATCHES ** | 1 |
| MAX START LATITUDE (DEG) ** | | .45000000000E+02 | | |
| ANTENNA I.D. ** | ANTENNA SPECIFICATION | MULTI-BEAM | PORESIGHT NADIR AT TO (DEG) ** | .20000000000E+02 |
| BOHESIGHT SQUINT AT TO (DEG) ** | | .34000000000E+02 | AZIMUTH ANGULAR COVERAGE (DEG) ** | .80000000000E+01 |
| ELEVATION ANGULAR COVERAGE (DEG) ** | | .30000000000E+01 | PHASE CENTER, BODY AXIS X (M) ** | 0. |
| PHASE CENTER, BODY AXIS Y (M) ** | | 0. | PHASE CENTER, BODY AXIS Z (M) ** | 0. |
| COORD SYS, BODY AXIS ROLL, (DEG) ** | | 0. | COORD SYS, BODY AXIS PITCH, (DEG) ** | -.70000000000E+02 |
| COORD SYS, BODY AXIS YAW, (DEG) ** | | .34000000000E+02 | PLAT ROLL RATE (DEG/S) ** | 0. |
| PLAT PITCH RATE (DEG/S) ** | | 0. | PLAT YAW RATE (DEG/S) ** | 0. |
| TEHRATE I.D. ** | TERRAIN SPECIFICATION | MULTI-11 | NO OF DISCRETES ** | 43 |
| NO OF FIELDS ** | | | 4 TOTAL NO OF SCATTERERS ** | 933 |
| X-AXIS COVERAGE (KM) ** | | .19984500000E+03 | Y-AXIS COVERAGE (KM) ** | .21300000000E+02 |
| TEHRATE CENTER, R (KM) ** | | .636/5192770E+04 | TERRAIN CENTER, LAT (DEG) ** | .45000000000E+02 |
| TEHRATE CENTER, LONG (DEG) ** | | .34020958470E+03 | | |
| SYNTHETIC ARRAY NC ** | SYNTHETIC ARRAY PARAMETERS | 1 | TRANSMISSION START TIME (S) ** | .75706842121E+03 |
| ARRAY LENGTH (M) ** | | .23947304242E+04 | ARRAY INCLINATION (DEG) ** | .81088631361E-01 |
| ARRAY FORMATION TIME (MS) ** | | .321/6541097E+03 | PLATFORM VELOCITY (KM/S) ** | .74580106359E+01 |
| NO OF PULSES ** | | 1758 FRF (HZ) ** | | .54629996835E+04 |
| NO OF RANGE SAMPLES ** | | 255 % OF AZIMUTH FILTERS ** | | 255 |
| PATCH CENTER RANGE SAMPLE NC. ** | | 128 PLAT RANGE SWATH WIDTH (KM) ** | | .24510624417E+01 |
| SLANT RANGE RESOLUTION (M) ** | | .19224146775E+02 | PLAT RANGE SAMPLE INTERVAL (M) ** | .96120733877E+01 |
| START RANGE (KM) ** | | .86659032998E+03 | RANGE PATCH CENTER (KM) ** | .86781106330E+03 |
| SG INT ANGLE PATCH CENTER (DEG) ** | | .341/5164252E+02 | NADIR ANGLE PATCH CENTER (DEG) ** | .19946775461E+02 |
| LOS AZIMUTH AT PATCH CENTER (DEG) ** | | .17017585118E+03 | LOS INCIDENCE AT PATCH CENTER (DEG) ** | .22611644021E+02 |
| PATCH CENTER, R (KM) ** | | .636/5192770E+04 | ORBITER MASS CENTER, R (KM) ** | .71763842359E+04 |
| PATCH CENTER, LAT (DEG) ** | | .45000000000E+02 | ORBITER MASS CENTER, LAT (DEG) ** | .42372508999E+02 |
| PATCH CENTER, LONG (DEG) ** | | .34020958470E+03 | ORBITER MASS CENTER, LONG (DEG) ** | .33959432948E+03 |

FIGURE 9

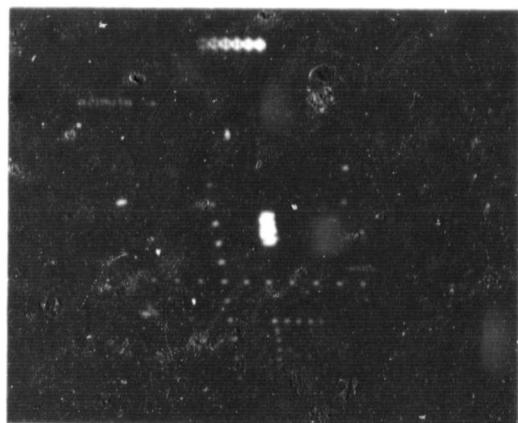
SARCON DATA - MULTIBEAM MODEL 2

ORIGINAL PAGE IS
OF POOR QUALITY



(a)

2 dB/GRAY SCALE - 16 SCALES



(b)

2 dB/GRAY SCALE - TOP 6 SCALES

FIGURE 10
IMAGES FROM THE SECOND MULTIBEAM SIMULATION

instead of being composed strictly of point scatterers. The skewing in the azimuth direction discussed above for the first model is more evident in this model. The skewing also caused the scatterers in the extreme left top and bottom right of the terrain model to be pushed off the image, and they do not appear in the photographs of Fig. 10. Reference 1 includes photographs (see Ref. 1, p. 11/2) of images produced under the test simulation which that document describes. That test simulation and the simulations described in this report contain some identical parameters, i.e., wavelength, orbit specification, and planet specification. The multibeam simulations were squint mode simulations (as opposed to sidelooking) and the synthetic array formation parameters are different for the models. The images shown on page 11/2 of Ref. 1 contains a scatterer of amplitude 26 dB above the calibration target just as the second multibeam simulation model does. However, the test simulation shows the large discrete target to have much higher sidelobes than the multibeam models; the higher PRF and multibeam processing appear to suppress the sidelobes even though the same azimuth weighting functions are used.

VI. CONCLUSIONS

While some concessions had to be made in adapting the OSS to implement the wideswath multibeam SAR technique, the basic concept was successfully incorporated into the OSS for verification. Overall, the OSS proved to be versatile and, in particular, was completely (and efficiently) adapted to the task of generating synthetic I/Q video data from a multiple antenna element orbital SAR model.

The multibeam technique for generating wideswath SAR images has been verified. No serious design problems were encountered in the implementation of the multibeam technique. However, the advantages of the technique compared to conventional SAR image techniques are still not completely clear. The multibeam technique allows for higher PRF's, implying lower transmitter peak power and greater Doppler ambiguity suppression, but the possible advantages in wideswath image formation and registration are still not clear. A study of signal processing and image formation algorithms and the development of a Doppler processor incorporating multiple beams and the multibeam geometry would be necessary to adequately address the possible advantages. Also a study of the effects of antenna array and platform errors on the formation of multibeams (using the OSS-multibeam simulation) would prove useful.

APPENDIX A
LISTING OF PROGRAM MECHO

PRECEDING PAGE BLANK NOT FILMED

PROGRAM MFCHN 73/171 NPT=2

FTN 4.8+528 82/09/07. 16.06.42

```
PROGRAM MECHO(SARCN=0, TDATA=0, ADATA=0, ANTPS=0, EDATA=0, PLOT,
1 INPUT, OUTPUT, TAPE25=0)
COMMON SARCN, PI, TPI, PIH, RIU, DTR, CL
COMMON KELT, PHF, PFE, PGR, PRA, PTM
COMMON KORP, OSMA, CE, OTNC, OLON, OPERI, UTP, ORA, TINIT, XEC
COMMON KUACP, WL, THW, SNR, LRC, LPT, KPC, KPS, RESH, RFSA, SRD, SRA,
•KFTNR, KWFTNA, SHADFA, PCOFF, PCOFFA, SW, NA, STLAT
COMMON KANT, SNAC, SQUINT, ARW, ERW, PHCPH(3), DPDY(3),
COMMON KSCNC, NDISC, AFNS, NSCATS, EMEAN, UISTX, DISTY, TCP, TCLA,
•TCP, LONG
COMMON IO, PPF, PRFCMD, NP, NF, NRA, RMIN, SHSW, RFSSW, SISB, IOHPC
COMMON LAATO, AL, AT, PLATP(3), PPMAG, PLATV(3), PVIMAG, SHPR, XSUPC,
•XNAPC, GAMMA, XA2PC, XIAPC, APC, PCR, PCLNG, SR, SLAT, SLONS
COMMON PHCP(3), F, HS, SARCON2
COMMON /ATPAT/KANIP, MDAZ, DAZ, ANTZA(100), MIDL, DEL, ANTEL(100),
COMMON /THEAD/KSNOK, NDTSCK, NFLDSX, NSCATSX, EMEANX, DISTX,
•DISTY, NRECS
DIMENSION SPRL(2*258*16), TERRAIN(4,256)*A(3)*ANTD(2007)*LBL(2)
DIMENSION PHCPBX(16), PHCPBY(16), PHCPBZ(16), X(16), Y(16), Z(16)
EQUIVALENCE (KANTP), ANTR(1)
C***** ECHO -- COMPUTES SLANT RANGE AND ECHO LEVEL OF EACH SCATTERER
C*** FOR EACH PULSE FOR EACH ANTENNA ON THE ORBITER AND STORES IN
C*** PULSE Sequence, ALL SCATTERERS EACH PULSE, AT 256 SCATTERERS OR
C*** LESS PER RECORD, IN ARRAYS PER FILE.
C*** SARCON- SARCON DATA, INPUT.
C*** IDATA- TEPHAIN DATA, INPUT.
C*** ANATA- ANTENNA PATTERN DATA, INPUT.
C*** ANTPS- ANTENNA POSITION DATA, INPUT.
C*** EDATA- SLANT RANGE, ECHO STRENGTH DATA, OUTPUT.
C*** TAPE25- TERRAIN DATA, TEMPORARY.
C***
```

```
ITFRX=0
1 PRINT 1110, $ IPULSE=IFLG3=IFLG4=IPNLNY=0
   NASKP=NPSKP=U
   ITFRX=ITFRX+1   IF (ITFRX.GT.1) GOTO 10
   PRINT *,-,----- PROGRAM MFCHO IN EXECUTION -----
10 IF (LIGHIF(5).EQ.0) PRINT *,-,# INPUT KBANCH#
   READ *, KHRANCH
```

35

ORIGINAL PAGE
OF POOR QUALITY

PROGRAM MECHO

73/171 OPT=2

82/09/07. 16.06.47

FTN 4.4+578

```
45      IF (EOF (.I INPUT) .NE. 0.0) GOTO 1000  
      IF (KBRANCH.FQ. .NE. SARDATA.) GOTO 100  
      IF (KBRANCH.FQ. .NE. TEHDATA.) GOTO 200  
      IF (KBRANCH.FQ. .NE. PLD.) GOTO 250  
      IF (KBRANCH.FQ. .NE. ANIDA.) GOTO 300  
      IF (KBRANCH.FQ. .NE. PRUCFS.) GOTO 400  
      IF (KBRANCH.FQ. .NE. AECOVERPAGE.) GOTO 320  
      IF (KBRANCH.FQ. .NE. PDHPY.) GOTO 360  
      IF (KBRANCH.FQ. .NE. PRFMAN.) GOTO 380  
      IF (KBRANCH.FQ. .NE. PAPEND.) GOTO 390  
      GOTO 10  
C*** SARDATA -- IDENTIFY SARDATA DATA FILE NO.  
C*** IFILS- FILE NO.  
100 CONTINUE  
LUNSA=.LSARCON# $ LUNS=.GLSARCON  
IF (LIGHTF(5).EQ.0) PRINT * ,# INPUT IFILS#  
READ *, IFILS  
PRINT 1010,LUNSH,IFILS  
IRFC=0  
CALL LUNPOS(LUNS,IFILS)  
GOTO 10  
C*** TERRATA -- IDENTIFY TERRAIN DATA FILE NO.  
C*** IFILT- FILE NO.  
C*** XY7SCAL- SCALE FACTOR APPLIED TO TERRAIN DATA (KM).  
200 CONTINUE  
LUNTA=.LTDATA# $ LUNT=.SLTDATA  
IF (LIGHTF(5).EQ.0) PRINT * ,# INPUT IFILT,XY7SCAL#  
READ *, IFILT,XY7SCAL  
PRINT 1020,LUNTR,IFILT  
PRINT *,XY7SCAL,* KM SCALE FACTOR APPLIED TO TERRAIN DATA.*#  
IRFC=0  
CALL LUNPOS(LUNT,IFILT)  
GOTO 10  
C*** PLNT -- PLOT SLANT RANGE, ECHO LEVEL DATA.  
C*** IPULSE- PULSE NO.  
C*** TARAY- ARRAY NO.  
C*** IPONLY- PLOT ONLY FLAG IF = 1. OTHERWISE NORMAL ECHO DATA  
C*** OUTPUT FILE WRTTFN.  
250 CONTINUE
```

PROGRAM MFCHO 73/171 OPT=2 FTN 4.8+528 82/09/07. 16.06.42

```

      IF (LIGHIF(5).EQ.0) PRINT *,* INPUT IPULSE,IARAY,IPONLY#
      REAN *,IPULSE,IARAY,IPONLY
      PRINT 1070,IPULSF,IARAY
      IF (IPONLY.EQ.1) PRINT *,*PLOT ONLY. NO OTHER OUTPUT.*#
      IF (LFN.EQ.4) PLOT GOTO 260
      LFN=4LPLNT $ CALL PLTFN(LFN,*K GRAF#)
260   CALL PLINRG(2.,4.)
      GOTO 10
C**** ANTDATA - IDENTIFY ANTENNA PATTERN DATA FILE NO.
C**** FILA- FILE NO.
      CONTINUE
300   LUNAR=FANATA# $ LUNA=SLADATA
      IF (LIGHIF(5).EQ.0) PRINT *,* INPUT IFILA#
      READ *,IFILA
      PRINT 1030,LUNAH,IFILA
      IRECA=0
      CALL LUNPOS(LUNA,IFILA)
      GOTO 10
C*** ACOVERAGE -- CHANGE ANTENNA COVERAGE IN AZIMUTH AND ELEVATION.
C*** SARCON WORDS ABW,FBW.
      CONTINUE
320   IF (LIGHIF(5).EQ.0) PRINT *,* INPUT ABW,FBW (DEG)#
      READ *,ABW,FBW
      PRINT 1040,ABWX,FBWX
      IF (FLG1=1 $ GOTO 10
C*** PDPRY -- CHANGE PLATFORM RATES OF ROLL,PITCH,YAW.
C*** SARCON ARRAY PDPRY.
      CONTINUE
350   IF (LIGHIF(5).EQ.0) PRINT *,* INPUT PDPRY(3) (DEG/S)#
      READ *,PDPRYR,PDPRYP,PDPRYY
      PRINT 1100,PDPRYR,PDPRYP,PDPRYY
      IF (FLG3=1 $ GOTO 10
C*** PRFMAN -- MANUAL PRF INPUT. SARCON WORD PRF.
      CONTINUE
380   IF (LIGHIF(5).EQ.0) PRINT *,* INPUT PRF#
      READ *,PRFMAN
      PRINT *,*PRF CHANGED TO *PRFMAN
      IF (FLG4=1 $ GOTO 10
C*** APPEND -- APPEND PROCESSING.

```

PROGRAM MECHO

FTN 4.0+528

82/09/07. 16.06.4;

```

C**** NASKP= NC. OF ARRAYS TO SKIP ON FILES SARCON AND
C**** LDATA. NPSKP= NC. OF PULSES TO SKIP ON FILE EDATA.
125      390 CONTINUE
          IF (LIGHIF (5).EQ.0) PRINT 402 INPUT NASKP.NPSKP#
          RFAN * .NASKP.NPSKP
          PRINT 403 APPEND PROCESSING. SKIP * .NASKP.* ARRAYS. THEN * .
          NPSKP.* PULSES.*#
          GOTO 10

C**** PROCESS -- GENERATE OUTPUT FILE OF SLANT RANGE. ECHO LEVEL DATA
C**** FOR EACH SCATTERER, FOR EACH PULSE, FOR EACH ARRAY.
C**** FILE NO.
130      400 CONTINUE
          LUNREC=EDATA# $ LUNSRE=SLNEDATA
          IF (LIGHIF (5).EQ.0) PRINT 404 INPUT IFILSRE#
          READ * .IFILSRE
          PRINT 1040.LUNSRE# .IFILSRE
          TRECSE=0 $ CALL LUNPOS(LUNSRE,IFILSRE)
          IPSARCNE=2

C**** READ AND STORE ANTENNA PATTERN DATA.
          IRFCA=IRFCA+1
          RUFFER IN(LINA,1) (ANID(1),ANTD(2007))
          TF (INIT(LINA))410.408.406
          406 STOP #P.F. ON LUNA#
          408 PRINT 1050.LUNAR.IRFCA $ GOTO 10
C**** ARRAY LOOP START. RFAN SARCON DATA.
          410 CONTINUE
          IRFCS=IRFCS+1
          RUFFER IN(LINIS,1) (SARCON1,SARCON2)
          IF (INIT(LUNIS))416.415.414
          414 STOP #P.F. ON LUNIS#
          415 PRINT 1050.LUNIS.IRFCS $ GOTO 10

135      416 CONTINUE
          C**** UPDATE SARCON DATA.
          KANTEKANTP
          IF (TFLG1.EC.0) GOTO 417
          IF (TFLG1.EC.0) GOTO 417
          AHW=AHWA*DTR $ ERW=ERWX*DTR $ CALL PRFSRCT(0.)
          C**** INIT ANTENNA PHASE CENTER POSITIONS FROM FILE - ANTPAS .
          417 CONTINUE

```

ORIGINAL PAGE IS
OF POOR QUALITY

PROGRAM MECHO

73/171 OPT=2

FTN 4.8.528

82/09/07. 16.06.4:

```

LUNAPOS=ALANIPOS          157
READ(LUNAPCS,*),NANTS      158
DO 2417 IL=1,NANTS         159
2417 READ(LUNAPOS,*),PHCPBX(JL),PHCPBY(JL),PHCPBZ(JL)
REWIND LUNAPOS              160
41A IF(FLGJ.EQ.0)GOTO 419
PDRPY(1)=PDPYY*DIR $ PDRPY(2)=PDRYP*DIR
PDRPY(3)=PDPYY*DIR
419 IF(FLGJ.EQ.0)GOTO 409
CALL PR-SLCT(PRFMAN,
C*** READ TEMPAIN DATA CN FIRST ARRAY. RESCALF. ROTATE FROM ENU,
C*** CONVERT TO GREFNwICH TOD, RESTORE.
409 IF(ITA.EU.1)420,440
420 IRFCT=IMFCI*1
RUFFER IN(LINT,1)(KSNoy,NRECS)
IF(LINIT(LINT))423,422,421
421 STOP #P.F. ON LUNIT#
422 PRINT 1050, LUNIT,IRECT $ GOTO 10
423 TCPx=PCX $ TCLAIx=PCLAT $ TCLONGx=PCLONG
DISTXX=UTSTxx*XY7SCAL $ DISTYX=DISIYx*XY7SCAL
NSCATR=128
DO 430 IPECS=1,NRECS
IF(IPECS.EQ.NRECS)NSCATR=NSCATSx-(NRECS-1)*NSCATR
NWDS=NSCATR*4
IRFCT=IMFCI*1
RUFFER IN(LINT,1)(TERATN(1)*TERAIN(MWDS))
TF(LINIT(LUNIT))426,425,424
424 STOP #P.F. ON LUNIT#
425 PRINT 1050, LUNIT,IRECT $ GOTO 10
426 CONTINUE
DO 428 NSCATR=1,NSCATP
DO 427 I=1,3
427 A(1)=TERAIN(1,ISCAIR)*XYZSCAL
CALL R017(A,XA7PC-PI);
A(3)=A(3)*TCRX
CALL ROTX(A*TCLATX-PIH)
CALL ROTX(A*-PIH-TCLONGX)
CALL XY/TSPH(A,A) $ A(1)=PRADIUS(A(2)) $ CALL SPHTXYZ(A,A)
DO 428 I=1,3

```

PROGRAM MECHN

73/171 OPT=2

82/09/07 • 16.06.4:

FTN 4.R+528

```

428 TEPAIN(1,ISCATP)=A(I)
RUFFR UNT(25,1) (TERAIN(1),TERAIN(NWUS))
TF ((INIT(P5))430.4<9.420
429 STOP #P.F. ON 25#
430 CONTINUE
205 ENDFILE 25
CALL AMHTL((MATLA•UATLF)
IF ((TPULSF.EQ.0) GOTO 440
XNPB=NRM $ DELTA=1.0
OFST=4.0/(XNPB-1.) $ I1=NRB/2
LRL(1)=#FCM LEVEL#
CALL PLAXTS(-OFSI•0•0•1•90•0•0•1•0•1•LRL•10•1•04••0R)
LRL(1)=#PANGE SAMP# $ LRL(2)=#LE#
CALI PLAXIS(0•0•4•0•0•1•XNR•DELIA,LBL,-12•I1•04••08)
440 CONTINUE
KSN0=KSNOX $ NDISC=NDISCX $ NFLDS=NFLDS $ NSCATS=NDCATSX
FMEAN=EMFANX $ DISTX=DISTXX $ DISTY=DISTYX
TCR=TCRA $ TCLA=TCLATX $ TCLONG=TCLONGX
C*** WRITE SARCON DATA.
IF ((NSKP.GF.IA)435•436
435 NRSKP=N#•(NRECS11)/2•1 $ CALL SKIPR(LUNSRE•0•NRSKP)
IRECSRE=IRECSRE+NHSKP $ GOTO 475
436 IF (TPONLY.EQ.1) GOTO 447 $ IF (NPSKP.GT.0) GOTO 442
DO 7442 IL=1,NANTS
PHCPB(1)=PHCPBX(JL) $ PHCPB(?)=PHCPHY(JL) $ PHCPR(3)=PHCPZ(JL)
IF (LIGHIF(6).EQ.0) CALL PSARCON(IPSARCN)
IRECSRE=IRECSRE+1
BUFFER UNT(LUNSRE•1) (SARCON)•SARCON2)
IF ((INIT(1)UNSRF))2442•441,441
225 441 STOP #P.F. ON LUNSRE#
2442 CONTINUE
442 CONTINUE
IP$ARCN=?
```

C*** PULSF LUMP START.

```

XIPP=1•0•PFR $ I=A10 $ IP1=1
TF (NPSKP.EQ.0) GOTO 433
NRSKP=NPSKP•(NRECS•1)/2•1 $ T=T•NPSKP•XIPP $ IP1=IP1•NPSKP
CALL SKIPER(LUNSRE•0•NRSKP) $ NPSKP=0
IRECSRE=IRECSRE+NRSKP
```

```

196 MECHO
197 MECHO
198 MECHO
199 MECHO
200 MECHO
201 MECHO
202 MECHO
203 MECHO
204 MECHO
205 MECHO
206 MECHO
207 MECHO
208 MECHO
209 MECHO
210 MECHO
211 MECHO
212 MECHO
213 MECHO
214 MECHO
215 MECHO
216 MECHO
217 MECHO
218 MECHO
219 MECHO
220 MECHO
221 MECHO
222 MECHO
223 MECHO
224 MECHO
225 MECHO
226 MECHO
227 MECHO
228 MECHO
229 MECHO
230 MECHO
231 MECHO
232 MECHO
233 MECHO
234 MECHO
```

ORIGINAL PAGE IS
OF POOR QUALITY

ORIGINAL PAGE IS
OF POOR QUALITY

```

PROGRAM MECHO          73/171   OPT=2           FTN 4.8+528      82/09/07. 16.06.41

23E      433 DO 470 IP=IP1,NP
          REWIND 25
          DO 434 JI=1,NANTS
          PHCP(1)=PHCPX(JL) $ PHCPB(?)=PHCPBY(JL) $ PHCPB(3)=PHLPBZ(JL)
          CALL PHLMOTN(T)
          X(JL)=PHRP(1) $ Y(JL)=PHCP(2) $ Z(JL)=PHCP(3)
          CONTINUE
          IF (LIGHTF(2).NE.1) GOTO 443
          IF (IA.NE.1) GOTO 443
          IF (IP.EQ.1) PRINT 1110
          IF (IP.LE.4) PRINT *,IA,IP,T,PHCP(3) *,IA,IP,T,X,Y
  434      443 NSCATR=128 $ NSCATR=0
          DO 460 IRECS=1,NRECS
          IOE=AND(IRECS,1)
          IF (IRECS.EQ.NRECS) NSCATR=NSCATR-(NRECS-1)*NSCATR
          NWDS=NSCATR*4
          IF (IOE.EQ.1) K2=0 $ K1=K2+1 $ K2=K1-1+NWDS
          BUFFER IN(25,1)(TERRAIN(K1),TERRAIN(K2))
          IF (UNIT(25)) 446,445,444
          444 STOP #P.F. ON 25#
          445 STOP #EOF CN 25#
          446 NSCATR=JSCATR+NSCATR
          IF (IRECS.NE.1) GOTO 449
          IF (TERRAIN(1)=PCH $ TERRAIN(2)=PCLAT $ TERRAIN(3)=PCLONG
              CALL SPHTXY7(TERRAIN,TPRAIN)
  449      IF (IRECS.EQ.NRECS) GOTO 447
          IF (IOE.EQ.1) GOTO 460
  447      DO 450 JI=1,NANTS
          DO 450 ISCATR=1,JSCATR
          RX=TERRAIN(1).ISCATH)-X(JL) $ RY=TERRAIN(2).ISCATR)-Y(JL)
          RZ=TERRAIN(3).ISCATH)-Z(JL)
          SRFL(1).ISCATR.JL)=SQRT(RX*RX+RY*RY+RZ*RZ)
          CALL ANINT(TERRAIN,SREL,JSCATR,T)
          DO 450 .IL=2,NANTS
          DO 450 ISCATR=1,JSCATR
          SREL(2).ISCATR.JL)=SREL(2).ISCATR.1
  450      IF (LIGHTF(2).NE.1) GOTO 451
          IF (IA.EQ.1) AND IP.LE.4 AND IRECS.LE.2) PRINT *,*ISCATR.*.
          *SRFL.TERRAIN #.(K*(SRFL(1).I=1,2),(TPRAIN(I,K).I=1,3).K=1,10)
  26E      27E

```

PROGRAM MECHO

FTN 4.8+528

82/09/07. 16.06.4:

```

C*** CHECK FOR DATA PLOT
 451 IF(IIP.NF.IIPULSE)GOTO 452
 451 IF(ITA.EU.JARAY)GOTO 500
 452 NWDSH=JSCATR*2 $ JSCATR=0 $ IF(IPONLY.EQ.1)GOTO 460
NWDSH=NWDS/2
DO 2460 JL=1*NANTS
TREC$RE=TREC$RE+1
RUFFER UNIT(LUNSRE,1)SREL(1,1,JL),SREL(2,NWDSH,JL)
IF(UNIT(LUNSRE)>460,455,455
STOP #P.F. ON LUNSRE#
2460 CONTINUE
460 CONTINUE
470 T=T*XIPP
475 IF(ITA.NE.NA)GOTO 410
ENDFILE IUNSRE $ PRINT 1060*LUNSRE,IREC$RE
480 IF(IPULSF.NE.0) CALL PLTEND(0.0)
GOTO 1
C*** PLNT SLANT RANGE, ECHO LEVEL DATA.
500 CONTINUE
DENOM=(NPB-1)*SISH/1000.
K=0 $ IF(TRECS.LE.21RO=SREL(1,1)
502 K=K+1 $ IF(K.GT.JSCATR)GOTO 510
XX=SREL(1,K)-R0*4./DNOM*2.
YY=SREL(2,K)
IF(XX.LT.0.0.RXX.GT.4.)GOTO 505
CALL PLI(XX,0,3) $ CALL PLT(XX,YY,2)
505 XX=SREL(1,K)-R0*4./DNOM*2. $ YY=SREL(2,K)
IF(XX.LT.0.0.RXX.GT.4.)GOTO 502
CALL PLI(XX,YY,3) $ CALL PLT(XX,0,2) $ GOTO 502
510 CONTINUE
IF(TRECS.EQ.NRECS.AND.IPOONLY.EQ.1)GOTO 480
GOTO 452
1000 CONTINUE
1010 FORMAT(* SARCON DATA ON *A10*, FILE*I3*.*)
1020 FORMAT(* TERRAIN DATA ON *A10*, FILE*I3*.*)
1030 FORMAT(* ANTENNA PATTERN DATA ON *A10*, FILE*I3*.*)
1040 FORMAT(* OUTPUT SLANT RANGE, ECHO LEVEL DATA TO BE WRITTEN ON *
1A10*, FILE*I3*.*)
```

ORIGINAL PAGE IS
OF POOR QUALITY

ORIGINAL PAGE IS
OF POOR QUALITY

| | | | | | |
|---------------|--------------------------|--|-------------|-----------|----------|
| PROGRAM MECHO | 73/171 | OPT=2 | FTN 4.8+528 | 82/09/07. | 16.06.42 |
| 315 | 1050 | FORMAT(* FCF SENSED ON *A10*, RECORD*I5*.*) | MECHO | 313 | |
| 316 | 1060 | FORMAT(* FOR WRITTEN ON *A10*, AFTER RECDR*D15*.*) | MECHO | 314 | |
| 317 | 1070 | FORMAT(* PLOT SR-EL DATA OF PULSE*D13*. ARRAY*D13*.*) | MECHO | 315 | |
| 318 | 1080 | FORMAT(* ANTENNA COVERAGE ABW,FRW CHANGED TO (DEG) -* | MECHO | 316 | |
| 319 | 12(1XE14.7) | | MECHO | 317 | |
| 320 | 1100 | FORMAT(* PLATFORM ATTITUDE RATE, PDRPY(3), CHANGED Tn* | MECHO | 318 | |
| 321 | 1* (DEG/S) -*3(1XE14.7), | | MECHO | 319 | |
| 322 | 1110 | FORMAT(*,*1*) | MECHO | 320 | |
| | END | | MECHO | | |

APPENDIX B
LISTING OF PROGRAM MBEAM

PRECEDING PAGE BLANK NOT FILMED

PHOTOGRAM WRF44W 73 / 77 OPT=2

FTN 4.8.528 82/09/07: 16.17.01

```

      COMMON WHEAT(INPUT,OUTPUT,IGNATA=0,IGNATL=0,IGNATR=0,
     1           INDATE=0,INDATE=0)
      COMMON SARC01,PI,TPI,PIH,RTR,NTP,CL
      COMMON KPLNT,SPF,PE,PER,PAR,PTW
      COMMON KORE,OZONE,OLON,PERI,UIP,CAR,TINIT,XER
      COMMON KADDP,EL,THW,SNP,LPC,LPK,KPCS,RFSR,SPD,SHA,
     *KPFTR,KWTFTH,LSHADE,P,COFFR,P,COFFA,SW,NA,SLAT
      COMMON KANT,SNAC,SGUIN,T,ABW,ERW,PHCPH,(3),ABPPY(3),
     *PDPY(3)
      COMMON KCNC,NMISC,NFLN,NSCATS,EMEAN,OUTSTX,DISTY,TCP,TCLAI,
     *TCI,NG
      COMMON IN,PDF,PRFWCD,NDP,NF,NRA,MIN,SHS,HESSH,SISR,1BHPC
      COMMON LA,ATO,AL,AT,PLATP(3),PPMAG,PLATV(3),PVWAG,SPPR,XSUPC,
     *XNADC,GAMMA,XA7PC,X1APC,APC,PCLAT,PCLCHG,SR,SLAT,SLONG
      COMMON PHCP(3),F,HS,SAPOCON2

```

```

***** PROGRAM TO FORM A REAM (SET OF I/Q DATA) IN THE RECEPTION
***** OF THE SOURCE AND READ ANGLES SPECIFIED IN THE SARCON DATA.
***** THREE AMF MANTS SETS OF INPUT DATA. EACH SET CONSISTING OF
***** THRE I/Q DATA COLLECTED FROM ONE ELEMENT IN THE ARRAY. IN LINE
***** 49, MANTS IS SET EQUAL TO 4, TO RUN A SIMULATION WITH A DIFFERENT
***** VALUE CHANGE THE VALUE OF MANTS AND IMF PROGRAM STATEMENT ACCORD-
***** INGLY. ALSO, THE ARRAY DIMENSIONS NEED TO BE CHANGED FOR SIMULA-
***** TIONS IN WHICH MANT IS GREATER THAN 255 AND/OR (MANT+1) IS NIANIS IS
***** GREATER THAN 1074.

***** EACH INPUT RECORD OF I/Q DATA IS OF LENGTH (NANT+1)*2 : EACH
***** RANGE BIN CONTAINS 2 SAMPLES - I AND Q DATA. THE ZENITH-1 TH
***** LORATION CONTAINS THE DISTANCE FROM THE ANTENNA ELEMENT PHASE
***** CENTER IN THE PATCH CENTER (SO THERE ARE MANTS DISTANCES +0 EACH
***** RECEIVED RADAR PULSE) AND IS USED FOR FOCUSING THE DATA IN EACH
***** PROGRAM. THE PHASE SHIFTS CALCULATED TO FORM THE REAM ARE PREFER-
***** ENCE TO THE FIRST ANTENNA ELEMENT (WHICH ALSO SERVED AS THE TRANS-
***** MITTING ANTENNA). THEREFORE THE FIRST ELEMENT PHASE CENTER IS
***** THE PHASE CENTER OF THE FORMED REAM AND THE DISTANCES FROM THE
***** FIRST ANTENNA ELEMENT TO THE PATCH CENTER ARE PUT IN THE OUTPUT
***** RECORDS OF THE REAM-FORMED I/Q DATA FOR USE IN THE FORMUSING
***** ROUTINES. ALSO THE SARCON RECORD FROM THE FIRST ELEMENT'S DATA
***** IS PLACED WITH THE REAM-FORMED DATA.

***** THE ANGLE OF THE ARRAY BORDERSIDE WITH RESPECT TO THE VELOCITY

```

43

PRECEDING PAGE BLANK NOT FILMED

PROGRAM MREAM 7,17] OPT=2 FTN 4.H+528 82/09/07. 16.17.0,

4: VECTOR (PHIN) AND THE INTER ELEMENT SPACING MUST BE ENTERED INTO
 5: THE PROGRAM INTERACTIVELY

6: INTEGER I (1,1 (4))
 7: REAL X(12048), Y(12048)
 8: COMPLEX CMPI(X,J),PSHIFT(4),EN(1024),EI(256)
 9: FQI,TVAL,UCE ((X1011),EN(1)), (X10REAM(1),EI(1))

10: NANTS=4
 11: LUN(1)=6LTODAT1 LUN(2)=6LTODAT2
 12: LUN(3)=6LTODAT3 LUN(4)=6LTODAT4
 13: LUN=LIGDATA
 14: CmplxJ=Cmplx(0.0,1.0)

15: READ THE SARCON RECORD OFF IQDATA AND SKIP THE ONES ON THE
 16: OTHER DATA SETS. THEN WRITE THE SARCON DATA UNTO
 17: OUTPUT FILE. IQDATA.

18: LUNTS=LUN(1)
 19: RUFFER IN ((LUNIS,1), (SARCON1,SARCON2))
 20: IF ((LUNIL(LUNIS)) .GT. 2n.10
 21: 10 STOP #P.F. ON LUNIL#
 22: 20 STOP #EOF ON SARCON INPUT#

23: 30 CONTINUE
 24: DO 31 JL=2,NANTS
 25: LUNTS=LUN(JL)
 26: CALL SKIPER(LUNIS,0,1,QLRINBUFFER)

27: 31 CONTINUE
 28: RUFFER OUT (LUNO,1), (SARCON1,SARCON2)
 29: IF ((LUNIL(LUNO)) .GT. 33,33

30: 33 PRINT *,P.F. ON LUNO - SARCON RECORD#
 31: STOP #P.F. ON LUNO - SARCON RECORD#

32: 37 CONTINUE

33: PRINT *,ENTER ANTENNA ELEMENT SPACING (N). PHI-0 (DEG) #,
 34: READ *,UH,PHI0
 35: PHIN=PHIN*CTR

ORIGINAL PAGE IS
OF POOR QUALITY

PROGRAM MHFAM 73/171 OPT=2

82/09/07. 16.17.0

FTN 4.8+528

```
      C***** CALCULATE THE PHASE SHIFT TO BE APPLIED TO EACH ELEMENT TO
      C***** SHIFT THF HFAM IN THE DIRECTION SPECIFIED BY THE SARCIN
      C***** DATA - SNAC1, SNAC.
      C
      C     ALPHA=TRI*CH* SIN(SMAC)*SIN(SQUINT-PHI10)/WL.
      C     DO 35 JL=1,NANTS
      C     PSHIFT(JL)=EXP(-CNPXL*(JL-1)*ALPHA)
      C     35 CONTINUE

      C***** READ, PROCESS HFAM FORMATION AND OUTPUT THF IQDATA FOR
      C***** THF FORMED READ.
      C
      C     IQWDS=(NRH+1)*?
      C
      C     DO 110 IP=1,NP
      C     CALL SE(XIOBEAM(1),XIOBEAM(IQWDS),0.)
      C     DO 60 JL=1,NANTS
      C     LUNIS=LUNI(JL)
      C     INDI=(JL-1)*IQWDS+1
      C     IND2=(IND1-1)*IQWUS
      C     RUFFER IN (LUNIS,1) (XIG(1),XIG(512))
      C     IF (LUNI(LUNIS)) 60,50,40
      C     40 STOP *P.F. ON INPUT - IQDATA#
      C     50 STOP *EOF ON INPUT - IQDATA#
      C     60 CONTINUE

      C     DO 100 IPH=1,NPH
      C***** CALCULATE AN I/O VALUE BY SUMMING THE PHASE SHIFTED I/O
      C***** DATA FROM EACH OF THE ELEMENTS ACROSS THE ARRAY.
      100  DO 100 IN=1,NANTS
      C     INDFX=IND+(I-1)*(NPH+1)
      C     EI(IPR)=EI(IPR)+EN(INDFX)*PSHIFT(IN)
      C     100 CONTINUE
      C     EI(NRH+1)=EN(NRH+1)

      C     RUFFER OUT (LUNO,1) (XIOBEAM(1),XIOBEAM(IQWDS))
      C     IF ((INI)(LUNO)) 110,105,105
      110  PRINT *,*P.F. ON LUNO - NP=NPH
```

ORIGINAL PAGE IS
OF POOR QUALITY

PROGRAM MHFAM 73/171 NPT=2

STOP STOP OK L1N0#
110 CONTINUE

STOP
END

FTN 4.0.H.528

82/09/07. 16.17.0e

REFERENCES

1. Gary L. Crow and Kermit E. Graf, "Imaging Radar Simulation and Signal Processing Software, Vol. I. An Orbital SAR Simulation Program," Applied Research Laboratories Technical Report No. 79-58 (ARL-TR-79-58), Applied Research Laboratories, The University of Texas at Austin, November 1979.
2. Buford Randall Jean, "Multiple Antenna Beam Techniques for Synthetic Aperture Radar," RSC Technical Report RSC-99, Remote Sensing Center, Texas A&M University, College Station, Texas, December 1978.
3. Ibid., p. 10.
4. Ibid., p. 58.
5. Ibid., p. 69.
6. Ibid., p. 85.
7. Ibid., p. 69.
8. Crow and Graf, op. cit.
9. Ibid., p. 5/6.
10. Ibid., p. 4/20.